Seismically imaging (continental) magma reservoirs



Rhyolitic magmatism at Yellowstone, Long Valley

Dacitic arc magmatism at Mount St. Helens



Mount St. Helens 1980
Eruptive volume



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¹now at Harvard University; ²now at Macquarie University



Seismically imaging (continental) magma reservoirs

Why?

Voluminous silicic eruptions require extensive geochemical evolution in the crust, which should leave an expression in seismic properties.

- How to identify the current life-cycle stage?
 - Where and how much magma is stored?
 - Geometry of transport pathways?
- Guidance for physical models

- Differences in magmatic system structure underlying eruptive characteristics (e.g., smaller and larger volume systems)?

Mount St. Helens

Long Valley & Yellowstone



Getting data – Broadband 3-C Seismographs





Justin Wilgus, Margaret Glasgow, Steve Hansen

Data are very versatile due to broadband and 3-C, but expensive and can only install a few per day at most. Once running, can collect long continuous time series

Rapidly deployable short-period and cable-free seismographs



Fairfield Nodal Zland

Autonomous seismographs or 'nodes': -cable-free

- -GPS clock
- -24-bit digitizer
- ~1 month battery life



Steve Hansen and Wes Thelen on the new dome at Mount St. Helens

The other way to deploy 1,000's of sensors...

Cabled geophones

Not feasible in rugged topography, urban areas, or areas that require low-impact





1,000 nodes

13 Students from U. New Mexicoand Portland State University2 field techs from NodalSeismic













Mount St. Helens Node Array in 2014



-122.3 -122.25 -122.2 -122.15 -122.1 -122.05

What are the measurable seismic wave properties that tell us about magmatic/volcanic structures?

 Speed (isotropic) from body wave travel times or group/phase speed

 Directionally dependent speed = anisotropic velocities

 Scattering – parent phase gives rise to new transmitted/reflected waves at sharp gradients in Vp, Vs

 Energy dissipation due to intrinsic attenuation





- k = Bulk modulus
- μ = Shear modulus
- $\rho = density$

$$\lambda = k - \frac{2}{3}\mu$$

 λ = Lame's lambda constant

What are the measurable seismic wave properties that tell us about magmatic/volcanic structures?

How to translate seismic properties into magmatic properties (bulk composition, temperature, melt, volatiles, etc)?





Chu et al. 2010 - melt effects tuned for Yellowstone

 $v_{p} = \sqrt{\frac{k + \frac{4\mu}{3}}{\rho}} = \sqrt{\frac{\lambda + 2\mu}{\rho}}$



- k = Bulk modulus $\mu = Shear modulus$
- $\rho = density$

$$\lambda = k - \frac{2}{3}\mu$$

 λ = Lame's lambda constant



d = Gm

Typically approached as an iterative linear inverse problem

- d = vector of travel time observations
- G = partial derivatives of each travel time with respect to a small change in each model parameter

m = vector of model parameters, slowness (1/velocity) in discrete volumes



Here, two ray paths sample a 3x3 model space

d = Gm



G = partial derivatives of each travel time with respect to a small change in each model parameter

m = vector of model parameters, slowness (1/velocity) in discrete volumes

Simple fake data

ray1 m1 m2 m3 m4 m5 m6 m7 m8 m9 ray2

d = [3.5 2.5] travel time in seconds

 $G = \left[\begin{array}{c} 1 \ 1 \ 1 \ 0 \ 0 \ 0 \ 0 \ 0 \\ 1 \ 0 \ 0 \ 1 \ 0 \ 0 \ 1 \ 0 \ 0 \end{array} \right]$

Rows = 2 observational ray paths Columns = 9 model parameters Length of ray path in each block controls sensitivity or $\delta t/\delta m$

 $m = 9 \times 1$ vector of slowness values

Least-squares optimal solutions can be found rapidly for very large systems

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Length of ray path in each block controls sensitivity or $\delta t/\delta m$

This simplification has proven useful, but such a severe approximation that sensitivity is limited to the source-receiver path is not accurate for most earthquake observations



Usually many more than 9 model parameters, especially for 3D



Global mantle scale example of P wave travel time sensitivity



For global scale tomography at period of ~2 s, sensitivity is ray-like given realistic dimensions of model parameters

At 20 s, the distribution of travel time sensitivity is substantially different and ray theory is a weaker approximation

(Dahlen et al., 2000; Hung et al., 2000)

Global mantle scale example of P wave travel time sensitivity





Off-path scattered energy can arrive close enough in time to the direct arrival to distort the waveform and influence the measured travel time (Assumes single-scattering)

Here sensitivity is calculated for a small perturbation to 1D reference model

It is more demanding to update these calculations of sensitivity with respect to a 3D reference model

(Dahlen et al., 2000; Hung et al., 2004)

Approaches to seismic tomography - travel times and finite frequency sensitivity kernels



42.42

42.41

Latitude (deg.)

42.40

42.39

body wave travel times to be meaningful

Reduces reliance on ad hoc smoothing constraints

Biryol et al., 2013

Recent/ongoing advances in tomography have largely proceeded in two different directions:

 Retain simple 1D assumptions for forward problem, but use computing power to sample highly multi-dimensional parameter space. Major benefit is uncertainty constraints.

2. Retain gradient based inversion, but use computing power to compute accurate 3D forward problem iteratively updating sensitivity kernels

Approaches to seismic tomography – Guided searching of parameter space

d = f(m)



Alternatively we can try <u>MANY</u> forward models and see which ones provides fit the data within their uncertainties

1D problems often need ~10 model parameters so this is a powerful way to obtain probabilistic results with simple forward problems

3D body wave problems often need $10^4 - 10^6$ parameters so this may be impractical or marginally possible with HPC (Burdick and Lekic, 2017)





[Shen et al., 2013]

Approaches to seismic tomography – Full Waveform Inversion

Here the sensitivity matrix G is updated with numerical calculation of full ~elastic wavefield. Each iteration is a HPC problem.

Application to southern California crust by Tape et al., 2009, 2010

Compromise is usually increased wavelengths for d

d = Gm

Dramatic increase in accuracy of G







Approaches to seismic tomography – Full Waveform Inversion

d = Gm

Compromise is usually increased wavelengths for d

Dramatic increase in accuracy of G

So far, early applications to continental magmatic systems just aim to fit surface wave dispersion at relatively long periods (e.g., Flinders et al., 2018) compared to signals generated by local earthquakes and controlled sources.

Lots of room to grow toward approaches more similar to those of the resource exploration industry (e.g., Yuan and Simons, 2014)



Industry benchmark model



Early, larger scale iteration updates smooth structure

Later iterations to fit finer scale body waves

Seismically imaging magma reservoirs,

starting with large systems at

Yellowstone and Long Valley

Mantle melt supply beneath Long Valley caldera

- Localized low-Vs uppermost mantle beneath LVC indicates continued source of partial melts from the mantle
- Inboard localization of plate boundary driven transtension drives mantle ascent





Mantle melt supply beneath Long Valley caldera

- Localized low-Vs uppermost mantle (<4.0 km/s) beneath LVC indicates continued source of partial melts from the mantle
- Inboard localization of plate boundary transtension drives mantle ascent





Jiang et al., 2018

P wave tomography at Long Valley



- Teleseismic P wave tomography with 3-D ray tracing
- Dense short-period array



Teleseismic P wave polarization evidence for very low velocity anomaly in upper-to-middle crust





Steck and Prothero, 1994

Long Valley cross-sections, different methods



 V_s perturbation from Walker Lane crust [%]

Full wave forward calculation

Inverts dispersion measurements for vertical component inter-station Greens function

Vsv reductions of ~20-30%, min Vs ~2.5 km/s (Flinders et al., 2018)



Flinders et al. 2018

Mantle source of Yellowstone

- Hot spot track with migrating onset of silicic magmatism
- Teleseismic S wave tomography
- Multi-scale broadband arrays



Schmandt et al., 2012

X'

Х

Mantle source of Yellowstone

- Hot spot track with migrating onset of silicic magmatism
- Teleseismic S wave tomography



Nelson and Grand, 2018

Yellowstone hotspot's crustal magmatic system



Yellowstone hotspot's crustal magmatic system



Two local minima in Vp perturbation as a function of depth

Low-mobility crystal-dominated mush with ~2-10% melt may be sufficient

Some waveform evidence for locally higher melt fractions of up to ~30% [Chu et al., 2010]



Polarization and waveform fitting in 2-D beneath Yellowstone caldera



Yellowstone hotspot's crustal magmatic system

Are these melt reservoirs uniform and well-mixed?

How does transport occur within and between them?

Does the mean velocity from tomography provide a good estimate of melt content and mobility?

Two local minima in Vp perturbation as a function of depth

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Rayleigh and Love waves



- V_{SV} & V_{SH} depend on the physical properties of rocks
- Inconsistency of Rayleigh and Love with a common Vs model indicates seismic anisotropy

Radial anisotropy and surface waves

- Oriented horizontally \rightarrow sills/lenses in magmatic context
- Oriented vertically \rightarrow dikes in magmatic context

Apparent anisotropy from layered isotropic media (e.g., Postma, 1955; Backus, 1962)



anisotropy

anisotropy

Seismic noise interferometry





Time window of signal recorded at A



Time window of signal recorded at B



Cross-correlations of A & B



 $\int u_1(t) u_2(t+\tau) dt = C(\tau)$
Signals emerge from longer-term averaging of cross-correlation functions



Empirical estimate of Green's function for a surface source

Bensen et al., GJI, 2007

Vertical and Transverse noise correlations at Long Valley



Wavefield from a 'virtual source'



Wavefield from a 'virtual source'



Focus on radial anisotropy in surface wave tomography

(mostly skipping earlier surface wave tomography steps)

Main steps:

- 1) Estimate empirical Green's function for ZZ and TT (using EE, NN, EN, NE)
- 2) Measure dispersion between station pairs for Rayleigh and Love waves
- 3) Invert dispersion curves for 2-D phase velocity maps
- 4) <u>Invert phase velocities for (an)isotropic Vs as a function of depth</u>





Inverting dispersion measurements for Vs(depth)

1,500,000 iterations per model point (based on tests of stability of posterior for anisotropic terms)

Posterior distribution defined as best 1,000 models at each location

Identify anisotropic parameters that are non-zero at 2-sigma





Influence of radial anisotrop parameters

Introduction of radial anisotropy leads to major improvements in fit to the dispersion data compared to isotropic inversions

Improvements are found in many areas, but some of the strongest are found beneath the calderas



Phase velocity uncertainty From repeated inversion with bootstrap resampling

Long Valley Caldera





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Phase velocity uncertainty From repeated inversion with bootstrap resampling



Where is anisotropy required at 1-2 sigma?



Radial anisotropy is most important to fitting middle crustal structure directly beneath the LV caldera

Long Valley region upper, middle, lower crust



Yellowstone region upper, middle, lower crust



Cross sections of anisotropic structures



Cross sections of anisotropic structures



Long Valley cross-sections, different methods



Jiang et al., 2018

Flinders et al. 2018

Origin of positive anisotropy in low-Vs volumes



Horizontally elongated volumes of partial melt \rightarrow magmatic sills/lenses?

Sill geometry tradeoffs



Sills of slow Vs (partial melt) embedded in faster host rock?

Best fit from 5-40% sills and 60-95% host rock And 1.6 – 2.4 km/s Vs in the sills (could be ~10-25% melt)



Negligible anisotropy beneath eastern Snake River Plain



V_{SH}<V_{SV}

Radial Anisotropy [%]

V_{SH}>V_{SV}

in the positive radial anisotropy volume

Growing seismic evidence for sill complexes beneath calderas from major silicic eruptions

Toba Caldera

Long Valley Caldera



At YS and LVC we can see the bottom of these sill complexes, indicating different reservoir characteristics where primitive melts first intrude the crust.

Very different tectonic/stress setting: active subduction (Toba), thin plate interior in transtension (LVC), craton undergoing slow extension (YS)

LVC Magmatic inflation centered at ~7-8 km





Montgomery-Brown et al., 2015

LVC Magmatic inflation centered at ~7-8 km



Are these large sill complexes the long-term magma reservoir, which rapidly mobilize into shallower more crystal-poor reservoirs before eruption (e.g., Rubin et al., 2017; Wotzlaw et al., 2015; Crowley et al., 2007; Till et al., 2015; Matthews et al., 2015)?

Similar depth relationship at Yellowstone, with inflation/deflation near top of sill complex (Chang et al., 2007)

Maintenance of compositional heterogeneity at Yellowstone



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Updated view for large volume silicic magmatic systems

Strong horizontal fabric consistent with middle-to-upper crustal melts in sill complex (~10-15% anisotropy)

Anisotropy affects estimates of melt volumes. Here, only using V_{sv} would lead to overestimation. But in-situ melt fractions in sills would be higher than the reservoir average.





Seismic view of large silicic magmatic systems

Strong horizontal fabric consistent with middle-to-upper crustal melt in sill complexes (~10% anisotropy)

Weaker or absent radial anisotropy in the lower crust indicates different melt storage geometry

Common depth-dependent anisotropic structure in areas with very different tectonic histories suggests dominance of young magmatic processes

(Cashman et al. 2017; Hildreth and Wilson, 2007)





Hunting for a relatively small magmatic system with lots of seismographs...

Mount St. Helens

Imaging Magma Under mt. St. Helens (iMUSH)

Seismic Investigators from:





Ken Creager, John Vidale, Geoff Abers, Alan Levander



Seth Moran, Wes Thelen

NODALSE

real cable free data acquisition

Late addition:





iMUSH Seismic Experiment





May 18th 1980 – Plinian eruption of MSH

~0.3 km³ ejected volume of dense rock equivalent

~300 m lower summit

(USGS)

ash/gas plume into stratosphere



Nichols et al., 2011

Seismicity time and depth distribution 1980-2014



Post-2009 small recharge episodes at Mount St. Helens?



Pacific Northwest Seismic Network

Some iMUSH structural imaging results:

Moho reflectivity - helps constrain magma plumbing location within the subduction system's thermal structure

Earthquake and active source travel time tomography – helps constrain current magma reservoir geometry

More from Geoff Abers this afternoon...

Offset Gathers^P

- PmP =
- 15-25 Hz bandpass
- 0.2 s short-term
- 1 s long-term
- Binned by distance
- Median trace



Normal Move Out (NMO) Shot Stacks





Hansen et al., 2016

Transportable Array Results





(Shen et al., 2013)



Mapping the extent of hydrated forearc mantle?



Westward migration of mantle melts beneath Mount St. Helens?



Thermal model from Syracuse et al., 2010 Seismic and Interp. From Hansen et al. 2016 ~700 °C, if edge of antigorite stability ~800 °C, if edge of chlorite stability
Controlled source P tomography using short-period array (~5000 geophone sites)



Eric Kiser et al., 2016, 2018 Geology

O

DLP Event

Pieces of the MSH plumbing system:

Result - Interpretation

Shallow vertical column of seismicity – conduit connecting shallow magma reservoir to surface

Upper crustal high Vp/Vs – shallow dacitic magma reservoir focused at same depths that fueled recent eruptions

Deep crustal low-velocity zone and contrast in Moho reflectivity - marks input of mantle melts east of MSH.





Pieces of the MSH plumbing system:

Result - Interpretation

Shallow vertical column of seismicity – conduit connecting shallow magma reservoir to surface

Upper crustal high Vp/Vs – shallow dacitic magma reservoir focused at same depths that fueled prior eruptions (Kiser et al., 2018)

Deep crustal low-velocity zone and contrast in Moho reflectivity - input of mantle melts east of MSH (Hansen et al., 2016).





Maren Wanke, Olivier Bachmann et al. at ETH

Questions/Topics

- Magma reservoir depths inferred from geophysical imaging, geodesy, and petrology (links to other lectures this week). How are they sensing different parts of the system or stages of the eruption life-cycle?
- How does melt organization change with depth, longevity of magmatic system, melt flux?
- Relating seismicity to magmatic system structure (more from Greg Waite, Diana Roman, Robin Matoza in later lectures).
- I neglected time-dependent structure constraints, but there are many interesting questions about magmatic sensitivity to small pressure or shear strain perturbations that could be partly addressed with seismology